

# Student Algebraic Geometry Seminar

Organizer(s): Andrew Critch and Andrew Dudzik

Fridays, 4:00–5:00pm, 740 Evans

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Fri, Apr 6 **Jason Ferguson**, UC Berkeley

*“Geometric” Properties of Schemes*

Many properties of schemes are preserved under base change. However, four properties of  $k$ -schemes that are not preserved under change of the base field  $k$  are reducedness, irreducibility, integrality, and connectedness. I will give examples, then define the notion of geometrically reduced, irreducible, integral, and connected  $k$ -scheme. Finally, I will then sketch a proof that to detect geometrically reducedness (resp. irreducibility, connectedness), it suffices to base change to the perfect closure of  $k$  (resp. separable closure of  $k$ , separable closure of  $k$ ). Along the way I will give some useful tricks for reducing statements about general  $k$ -schemes to finite-type  $k$ -schemes.

*After the seminar, everyone is invited out for drinks and dinner with the speaker.*